

Unit 4 Practice A - Solutions

Question	Points of expected responses	Illustrative scheme
1	<ul style="list-style-type: none"> •¹ use Section formula •² substitute •³ find coordinates of S 	<ul style="list-style-type: none"> •¹ $S = \frac{1}{7}(2t + 5r)$ •² $S = \frac{1}{7} \left(2 \begin{pmatrix} 3 \\ -7 \\ 2 \end{pmatrix} + 5 \begin{pmatrix} -4 \\ 7 \\ 5 \end{pmatrix} \right)$ •³ $S = (-2, 3, 3)$ <p>NB If candidates uses stepping out technique:</p> <ul style="list-style-type: none"> •¹ evidence of process •^{2,3} find coordinates of S
2	<ul style="list-style-type: none"> •¹ recognise a pathway for \overrightarrow{PT} •² identify $-\overrightarrow{SP}$ vector •³ complete calculation for \overrightarrow{PT} 	<ul style="list-style-type: none"> •¹ $\overrightarrow{PT} = -\overrightarrow{SP} + \overrightarrow{ST}$ •² $PS = -SP = -(6i - 10j - k)$ •³ $PT = (-6i + 10j + k) + (-2i + 4j + 4k)$ $= (-8i + 14j + 5k) \text{ or } \begin{pmatrix} -8 \\ 14 \\ 5 \end{pmatrix}$ <p>NB Do not award •³ for (-8, 14, 5).</p>
3	<ul style="list-style-type: none"> •¹ find vector components •² use scalar product •³ process scalar product •⁴ process \overrightarrow{PQ} and \overrightarrow{PR} ie calculate magnitudes •⁵ find angle 	<ul style="list-style-type: none"> •¹ $PQ = \begin{pmatrix} 0 \\ 4 \\ 6 \end{pmatrix}$ and $PR = \begin{pmatrix} -1 \\ 6 \\ -2 \end{pmatrix}$ •² $= \frac{\overrightarrow{PQ} \cdot \overrightarrow{PR}}{ \overrightarrow{PQ} \cdot \overrightarrow{PR} }$ •³ $PQ \cdot PR = (0 + 24 - 12) = 12$ •⁴ $PQ = \sqrt{52}$ and $PR = \sqrt{41}$ •⁵ angle = 74.94° radians or 1.31

4	<p>#2.1 select appropriate strategy to show collinearity</p> <ul style="list-style-type: none"> •¹ interpret vector •² interpret multiple of vector •³ complete proof •⁴ interpret ratio <p>#2.2 Explain a solution in context</p>	<p>#2.1 show they are collinear</p> <ul style="list-style-type: none"> •¹ eg $AB = \begin{pmatrix} 12 \\ -8 \\ 4 \end{pmatrix}$ •² eg $BC = \begin{pmatrix} 3 \\ -2 \\ 1 \end{pmatrix}$, $AB = 4BC$ •³ $AB = 4BC$ hence vectors are parallel, but B is a common point so A, B and C are collinear. •⁴ interpret ratio $AB : BC$, 4 : 1 <p>#2.2 Yes, the football coach has placed the cones correctly (with statement related to previous working).</p>
5	<ul style="list-style-type: none"> •¹ differentiates correctly 	<ul style="list-style-type: none"> •¹ $\frac{d}{dx} (4\sin x) = 4\cos x$
6	<ul style="list-style-type: none"> •¹ integrates correctly 	<ul style="list-style-type: none"> •¹ $3\sin\theta + c$
7	<ul style="list-style-type: none"> •¹ integrates correctly 	<ul style="list-style-type: none"> •¹ $h(x) = \frac{3}{4}(8 + x)^{\frac{4}{3}} + c$
8	<ul style="list-style-type: none"> •¹ starts integration •² completes integration •³ substitutes limits •⁴ evaluate definite integral 	<ul style="list-style-type: none"> •¹ $(x - 1)^4$ •² ... $x^{\frac{1}{4}}$ •³ $(\frac{1}{4}(2 - 1)^4) - (\frac{1}{4}(1 - 1)^4)$ •⁴ $\frac{1}{4} \text{ units}^2$
9 (a)	<ul style="list-style-type: none"> •¹ use $\log_a x + \log_a y = \log_a xy$ 	<ul style="list-style-type: none"> •¹ $\log_2(5p \times 7q) = \log_2 35pq$
(b)	<ul style="list-style-type: none"> •² $\log_a x^m = m \log_a x$ OR $\log_a x^m - \log_a x^n = \log_a \frac{x^m}{x^n}$ •³ simplify to $k \log_a x$ 	<ul style="list-style-type: none"> •² $8\log_a x - 5\log_a x$ OR $\log_a x^2$ •³ $3\log_a x$

10	<ul style="list-style-type: none"> •¹ starts to solve •² solves correctly 	<ul style="list-style-type: none"> •¹ $(x - 3) = 2^3$ •² $x = 11$ <p>NB if a candidate simply obtains the solution by inspection, award both points</p>
11	<ul style="list-style-type: none"> •¹ expand $k\cos(x - a)$ •² compare coefficients •³ process k •⁴ process a 	<ul style="list-style-type: none"> •¹ $k\cos x \cos a + k \sin x \sin a$ stated explicitly •² $k \cos a = 4$ and $k \sin a = 3$ stated explicitly •³ $k = \sqrt{25} = 5$ •⁴ $a = 36.89^\circ$
12	<p>#2.1 recognises that this has same shape as $10\cos(x + 36.9)$</p> <ul style="list-style-type: none"> •¹ sets up $\cos(\dots)$ correctly •² obtains compound angle •³ obtains double angle •⁴ obtains final angle 	<p>#2.1 evidence of the candidate using $10\cos(2x + 36.9)$</p> <ul style="list-style-type: none"> •¹ $\cos(2x + 36.9) = \frac{5}{10}$ •² $2x + 36.9 = 60^\circ, 300^\circ$ •³ $2x = 23.1^\circ, 263.1^\circ$ •⁴ $x = 11.55^\circ, 131.55^\circ$ reject 131.55° <p>NB award •⁴ only if 131.55° rejected</p>
		Total of 35marks plus 2 x #2.1 and 1 x #2.2